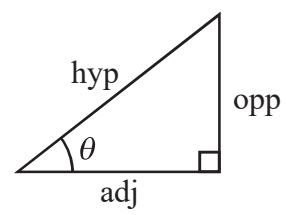
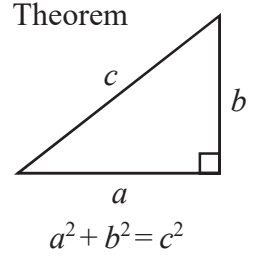


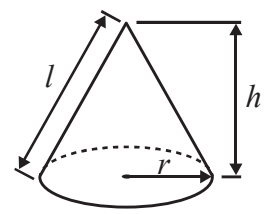
International GCSE MATHEMATICS FORMULAE SHEET – HIGHER TIER

Pythagoras' Theorem



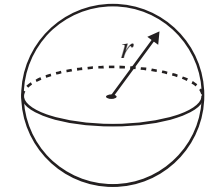
Volume of cone = $\frac{1}{3} \pi r^2 h$

Curved surface area of cone = $\pi r l$



Volume of sphere = $\frac{4}{3} \pi r^3$

Surface area of sphere = $4 \pi r^2$



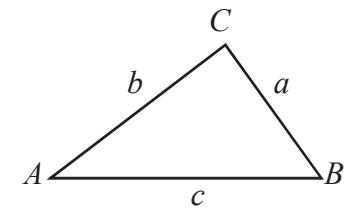
adj = hyp \times cos θ
opp = hyp \times sin θ
opp = adj \times tan θ

or $\sin \theta = \frac{\text{opp}}{\text{hyp}}$

$\cos \theta = \frac{\text{adj}}{\text{hyp}}$

$\tan \theta = \frac{\text{opp}}{\text{adj}}$

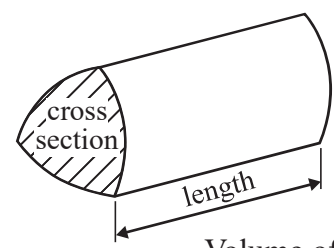
In any triangle ABC



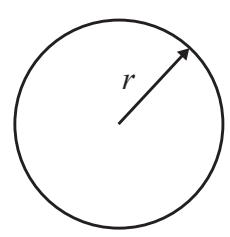
Sine rule: $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine rule: $a^2 = b^2 + c^2 - 2bc \cos A$

Area of triangle = $\frac{1}{2} ab \sin C$



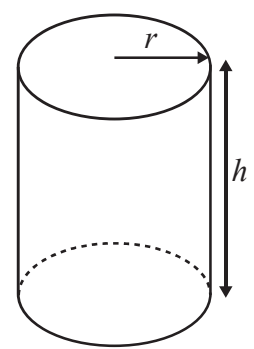
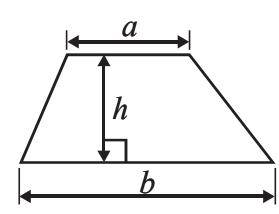
Volume of prism = area of cross section \times length



Circumference of circle = $2 \pi r$

Area of circle = πr^2

Area of a trapezium = $\frac{1}{2} (a + b) h$



Volume of cylinder = $\pi r^2 h$

Curved surface area of cylinder = $2 \pi r h$

The Quadratic Equation
The solutions of $ax^2 + bx + c = 0$,
where $a \neq 0$, are given by

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

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Answer ALL TWENTY TWO questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

- 1 Here are the ingredients needed to make 12 muffins.

Ingredients to make 12 muffins
300 g flour
150 g sugar
250 ml milk
100 g butter
2 eggs

Sarah makes 60 muffins.

- (a) Work out how much sugar she uses.

..... g
(2)

James makes some muffins.

He uses 625 ml of milk.

- (b) How many muffins did he make?

.....
(2)

(Total for Question 1 is 4 marks)

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2 $a = -5$
 $c = -2$

(a) Work out the value of $2a^2 + 6c$

.....
(2)

There are 4 pens in a small box of pens.
There are 10 pens in a large box of pens.

Ami buys x small boxes of pens and y large boxes of pens.
She buys a total of T pens.

(b) Write down a formula for T in terms of x and y .

.....
(3)

(Total for Question 2 is 5 marks)

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- 3 The table shows information about the number of visits each of 40 adults made to the gym last week.

Number of visits to the gym	Frequency
0	4
1	3
2	12
3	5
4	8
5	5
6	2
7	1

Work out the mean of the number of visits to the gym.

.....
(Total for Question 3 is 3 marks)

- 4 $A = \{2, 4, 6, 8, 10, 12, 14\}$
 $B = \{1, 3, 5, 7, 9, 11, 13\}$
 $C = \{3, 6, 9, 12\}$

(a) List the members of the set

(i) $A \cap C$

.....

(ii) $A \cup C$

.....

(2)

(b) Explain why $A \cap B = \emptyset$

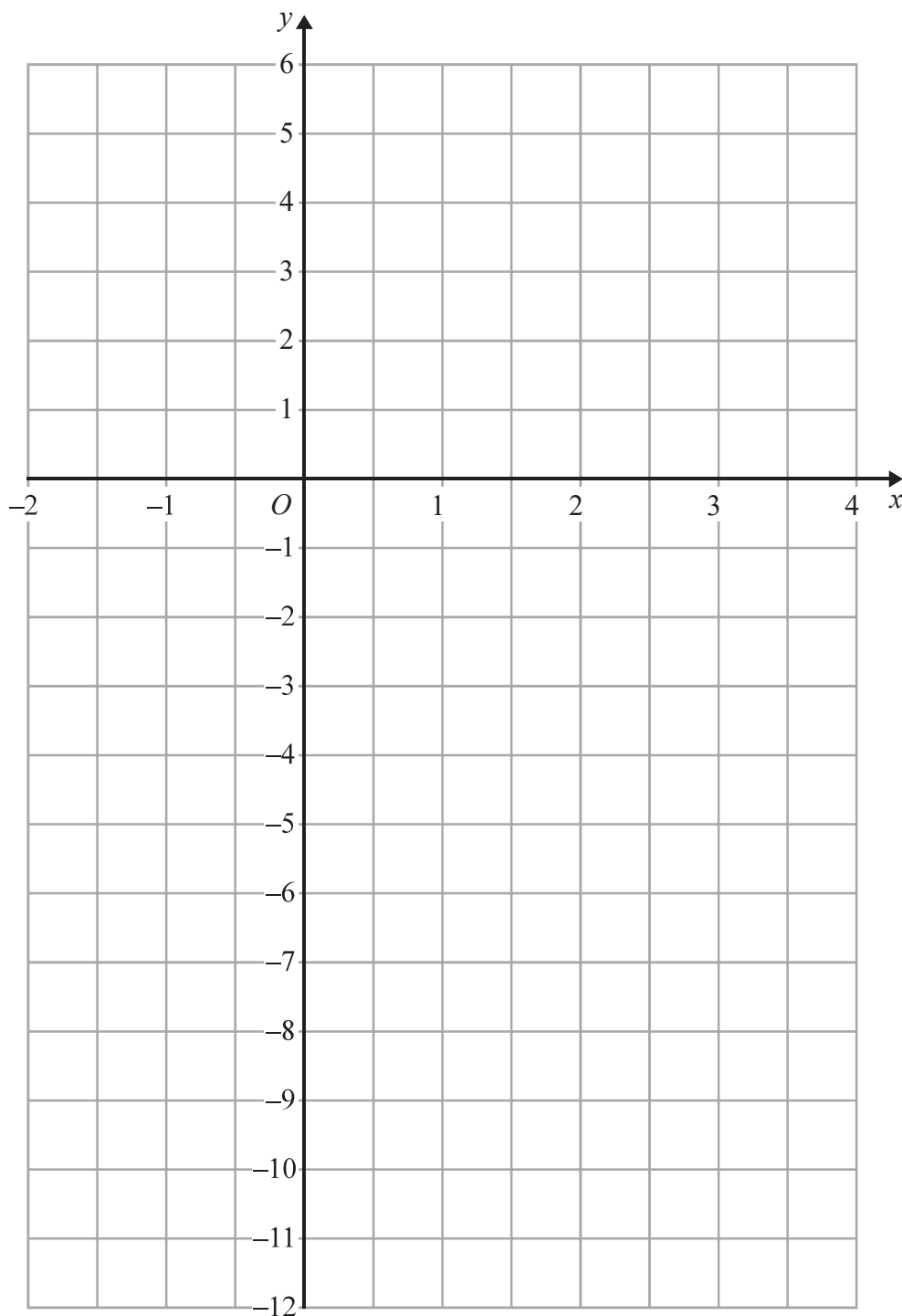
.....

(1)

(Total for Question 4 is 3 marks)



5 On the grid, draw the graph of $y = 3x - 5$ for values of x from -2 to 3



(Total for Question 5 is 4 marks)

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6 (a) Show that $\frac{3}{10} + \frac{2}{15} = \frac{13}{30}$

(2)

(b) Show that $2\frac{5}{8} \div 1\frac{1}{6} = 2\frac{1}{4}$

(3)

(Total for Question 6 is 5 marks)



7 (a) Factorise $3y^2 + 2y$

.....
(1)

(b) Expand and simplify $(x - 9)(x + 2)$

.....
(2)

(c) (i) Solve $6k + 5 < 20$

(ii) n is an integer and $6n + 5 < 20$

Write down the largest possible value of n

.....
(3)

(d) Simplify fully $\frac{28x^5y^3}{4xy^2}$

.....
(2)

(Total for Question 7 is 8 marks)

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8

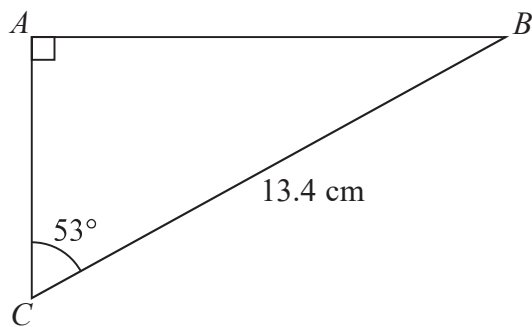


Diagram **NOT**
accurately drawn

Work out the length of AB .
Give your answer correct to 1 decimal place.

..... cm

(Total for Question 8 is 3 marks)

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P 4 5 8 4 1 A 0 9 2 4

9 Bhavin, Max and Imran share 6000 rupees in the ratios 2 : 3 : 7

Imran then gives $\frac{3}{5}$ of his share of the money to Bhavin.

What percentage of the 6000 rupees does Bhavin now have?

Give your answer correct to the nearest whole number.

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..... %

(Total for Question 9 is 5 marks)



10 The diagram shows a circle inside a rectangle.

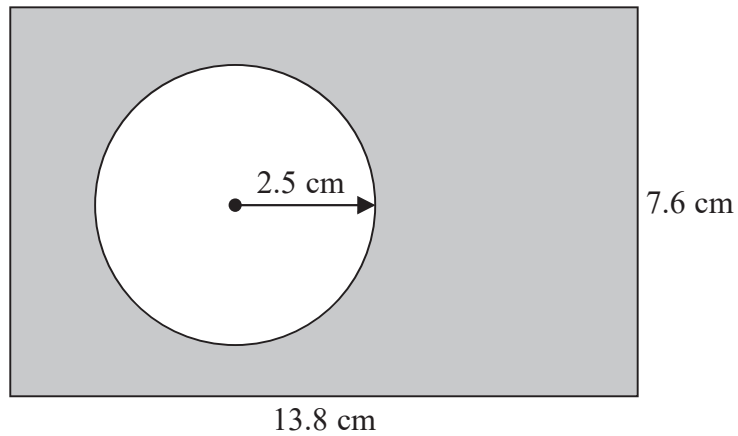


Diagram **NOT**
accurately drawn

Work out the area of the shaded region.
Give your answer correct to 3 significant figures.

..... cm²

(Total for Question 10 is 3 marks)

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11 The frequency table shows information about the weights of 80 adults.

Weight (w kg)	Frequency
$40 < w \leq 50$	4
$50 < w \leq 60$	7
$60 < w \leq 70$	21
$70 < w \leq 80$	21
$80 < w \leq 90$	18
$90 < w \leq 100$	7
$100 < w \leq 110$	2

(a) Complete the cumulative frequency table.

Weight (w kg)	Cumulative frequency
$40 < w \leq 50$	4
$40 < w \leq 60$	
$40 < w \leq 70$	
$40 < w \leq 80$	
$40 < w \leq 90$	
$40 < w \leq 100$	
$40 < w \leq 110$	

(1)

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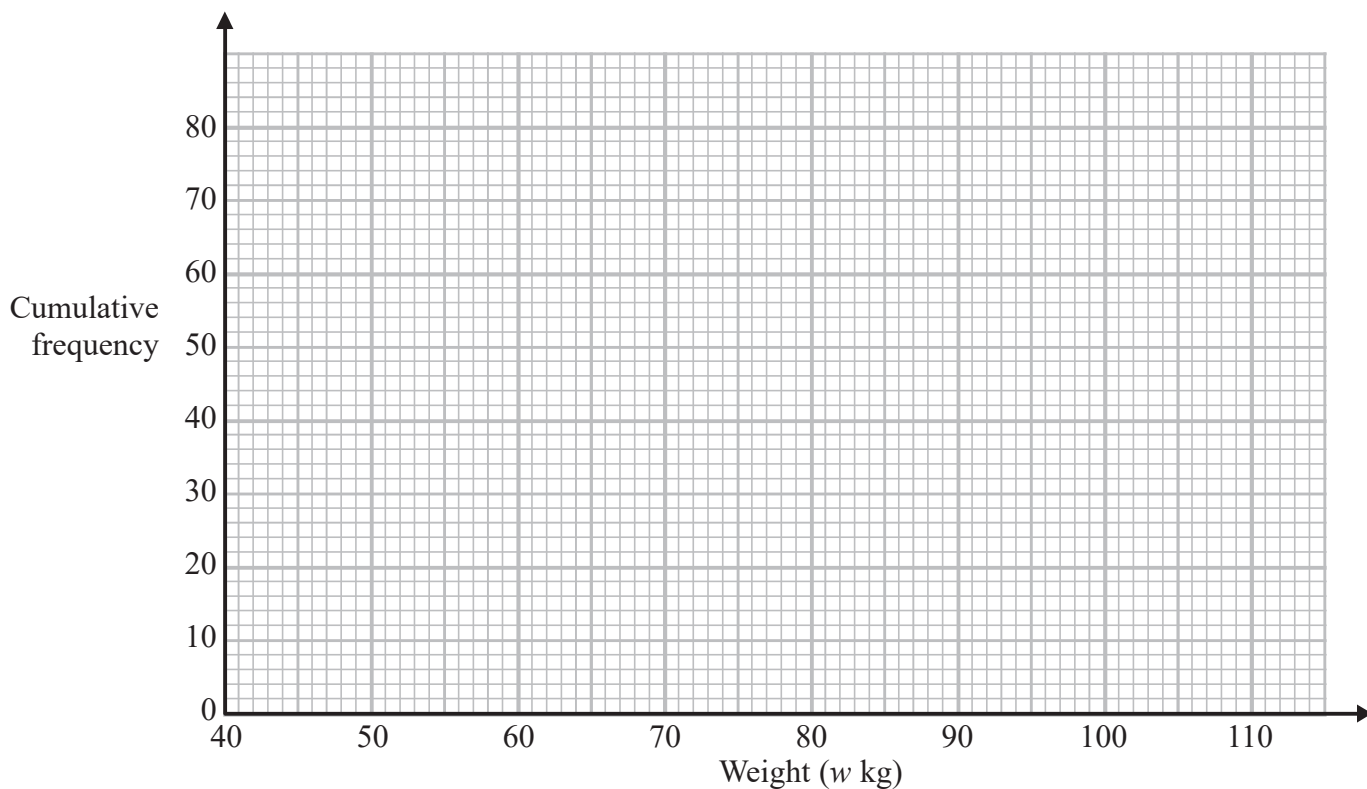
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(b) On the grid, draw a cumulative frequency graph for your table.

(2)



(c) Use your graph to find an estimate for the number of adults with weight more than 85 kg.

.....
(2)

(d) Use your graph to find an estimate for the interquartile range of the weights of the adults.

..... kg
(2)

(Total for Question 11 is 7 marks)



12 Solve the simultaneous equations

$$4x + 5y = 13$$

$$3x - 2y = 27$$

Show clear algebraic working.

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$$x = \dots\dots\dots$$

$$y = \dots\dots\dots$$

(Total for Question 12 is 4 marks)

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13 The straight line **L** passes through the points $(-2, 3)$ and $(6, 9)$

Find an equation of the line that is parallel to **L** and passes through the point $(5, -1)$
Give your answer in the form $ax + by = c$ where a , b and c are integers.

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.....
(Total for Question 13 is 5 marks)



- 14 A particle is moving along a straight line.
The fixed point O lies on this line.
The displacement of the particle from O at time t seconds is s metres where

$$s = 2t^3 - 12t^2 + 7t$$

- (a) Find an expression for the velocity, v m/s, of the particle at time t seconds.

$$v = \dots\dots\dots \text{ (2)}$$

- (b) Find the time at which the acceleration of the particle is instantaneously zero.

$$\dots\dots\dots \text{ seconds} \quad \text{(2)}$$

(Total for Question 14 is 4 marks)

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15 The diagram shows two mathematically similar vases, **A** and **B**.

Diagram **NOT**
accurately drawn



A



B

Vase **A** has a surface area of 120 cm^2

Vase **B** has a surface area of 750 cm^2 and a volume of 1600 cm^3

Work out the volume of vase **A**.

..... cm^3

(Total for Question 15 is 3 marks)

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16 $ABCDEFGH$ is a cuboid.

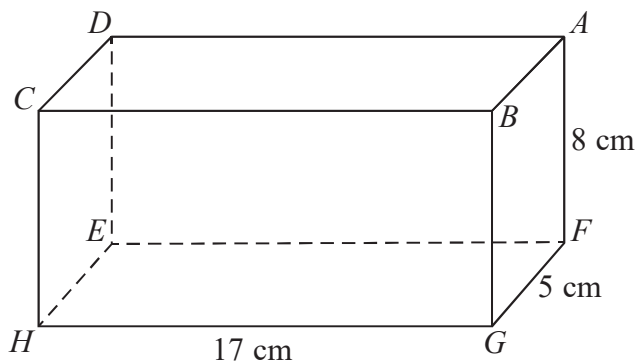


Diagram **NOT** accurately drawn

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The cuboid has

- length 17 cm
- width 5 cm
- height 8 cm

Work out the size of the angle that AH makes with the plane $EFGH$.
Give your answer correct to 1 decimal place.

.....

(Total for Question 16 is 4 marks)



17 The diagram shows a trapezium.

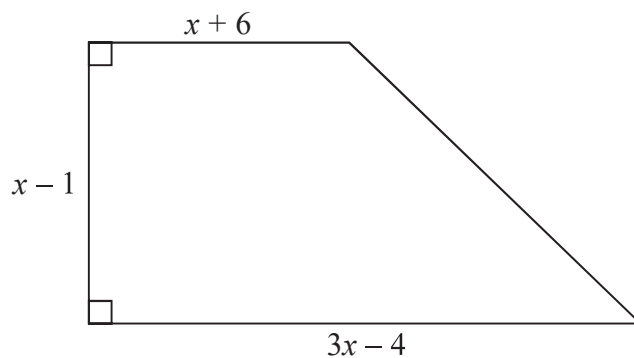


Diagram NOT
accurately drawn

All measurements on the diagram are in centimetres.

The area of the trapezium is 119 cm^2

(i) Show that $2x^2 - x - 120 = 0$

(ii) Find the value of x .
Show your working clearly.

$x = \dots\dots\dots$

(Total for Question 17 is 6 marks)

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18 Make t the subject of the formula $m = \frac{t+1}{t-3}$

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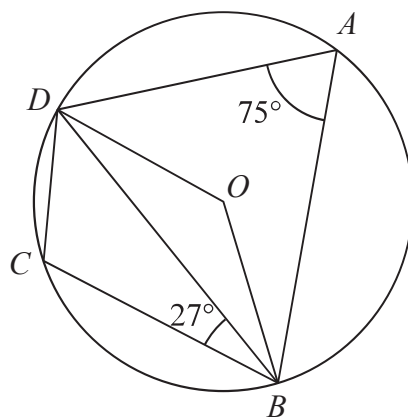
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.....
(Total for Question 18 is 4 marks)

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19

Diagram **NOT**
accurately drawn

A , B , C and D are points on a circle, centre O .

Angle $DAB = 75^\circ$

Angle $DBC = 27^\circ$

Work out the size of angle ODC .

.....
(Total for Question 19 is 4 marks)



P 4 5 8 4 1 A 0 2 1 2 4

20 A metal cube has sides of length 4.5 cm, correct to the nearest 0.5 cm.

The cube is melted down and the metal is used to make small spheres.
Each sphere has a radius of 3 mm, correct to the nearest millimetre.

Work out the greatest number of spheres that could be made from the metal.
Show your working clearly.

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.....
(Total for Question 20 is 5 marks)



- 21 There are 9 counters in a bag.
There is a number on each counter.



Kal takes at random 3 counters from the bag.

He adds together the numbers on the 3 counters to get his Total.

Work out the probability that his Total is 6

.....
(Total for Question 21 is 5 marks)



22 The diagram shows a pentagon.

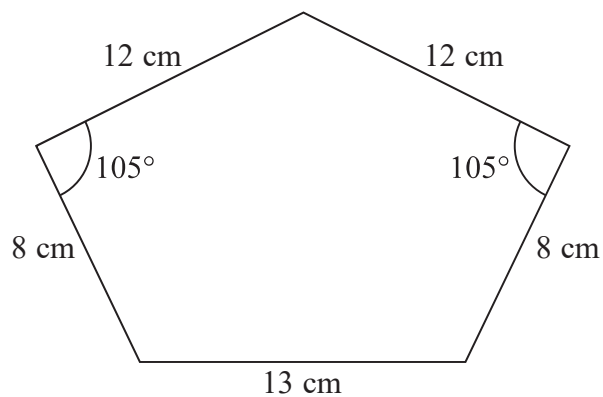


Diagram **NOT** accurately drawn

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Work out the area of the pentagon.
Give your answer correct to 3 significant figures.

..... cm²

(Total for Question 22 is 6 marks)

TOTAL FOR PAPER IS 100 MARKS

